

Regular article

# Solvent effects on the electronic absorption spectrum of formamide studied by a sequential Monte Carlo/quantum mechanical approach

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**Abstract.** Sequential Monte Carlo/quantum mechanical calculations are performed to study the solvent effects on the electronic absorption spectrum of formamide (FMA) in aqueous solution, varying from hydrogen bonds to the outer solvation shells. Full quantum-mechanical intermediate neglect of differential overlap/singly excited configuration interaction calculations are performed in the supermolecular structures generated by the Monte Carlo simulation. The largest calculation involves the ensemble average of 75 statistically uncorrelated quantum mechanical results obtained with the FMA solute surrounded by 150 water solvent molecules. We find that the  $n \rightarrow \pi^*$  transition suffers a blueshift of  $1,600 \text{ cm}^{-1}$  upon solvation and the  $\pi \rightarrow \pi^*$  transition undergoes a redshift of  $800 \text{ cm}^{-1}$ . On average, 1.5 hydrogen bonds are formed between FMA and water and these contribute with about 20% and about 30% of the total solvation shifts of the  $n \rightarrow \pi^*$  and  $\pi \rightarrow \pi^*$  transitions, respectively. The autocorrelation function of the energy is used to sample configurations from the Monte Carlo simulation, and the solvation shifts are shown to be converged values.

**Key words:** Formamide – QM/MM – Solvent effects – Absorption spectrum – Monte Carlo simulation

## 1 Introduction

The structural and spectroscopic changes of peptide groups ( $-\text{CONH}-$ ) upon solvation have been of great interest for a long time. This interest is related to the fact that peptides are the main repetitive units of polypeptide chains and proteins. Therefore, understanding how these groups can interact with each other and with the surrounding solvent molecules can give insight into the

complex intermolecular interactions that occur when proteins are solvated and also provide valuable information about the solvent effects on the structure and spectroscopic properties of these macromolecules.

With the aim of understanding the behavior of peptide groups in solution, several theoretical [1, 2, 3, 4, 5, 6, 7, 8, 9, 10] and experimental [11, 12, 13, 14] studies have been made on small peptide models such as *N*-methylacetamide,  $\text{CH}_3\text{CONHCH}_3$ , and formamide (FMA),  $\text{HCONH}_2$ . These works have focused mainly on the solvent effects on structural and vibrational properties; however, the study of the solvent effects on the electronic absorption spectra of peptide groups is sparse. The peptide group is the main chromophore of proteins, which has a weak  $n \rightarrow \pi^*$  transition at about 220 nm (about  $45,000 \text{ cm}^{-1}$ ) and a strong  $\pi \rightarrow \pi^*$  transition at about 195 nm (about  $51,000 \text{ cm}^{-1}$ ). The electronic transitions of most side chains occur below 200 nm and are masked by the intense  $\pi \rightarrow \pi^*$  transition of the peptide groups [15]. As a result, the electronic absorption spectra of proteins in solution will resemble those of small peptide models in solution. For instance, it has been shown that the electronic spectra of random-coil and  $\beta$ -strand proteins have spectra very similar to peptide models such as *N,N*-dimethylacetamide [15], with the  $\pi \rightarrow \pi^*$  absorption being redshifted. Time-resolved far-UV circular dichroism (CD) is today a powerful tool to monitor the pattern of the secondary structures of proteins [16]. The study of the normal electronic absorption spectrum of small peptide models plays an important role in obtaining good parameters for understanding the far-UV CD spectra of proteins [6, 7, 8, 9, 10, 17, 18].

The electronic spectrum of FMA in a vacuum is well understood [19] and comprises two Rydberg transitions, a weak  $n \rightarrow \pi^*$  transition, an intense transition from the nonbonding  $\pi_{\text{nb}}$  orbital  $\rightarrow \pi^*$  and a Q band, associated with the bonding  $\pi$  orbital  $\rightarrow \pi^*$ . However, the electronic spectrum of FMA in the condensed phase has not been studied extensively experimentally. From the theoretical point of view, the electronic spectrum of FMA has been studied in the gas phase [20, 21, 22, 23],

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in clusters with up to three explicitly included water molecules [9, 24, 25, 26] and clusters inside a cavity [9]. In an early study, Del Bene [24], observed a blueshift in the  $n \rightarrow \pi^*$  transition of FMA when complexed with one and two hydrogen-bonded water molecules. The magnitude of the blueshift was correlated with the strength of the hydrogen bond, which is weaker in the excited state. Sobolewski [25] has studied electronic transitions of FMA, involving the valence states, and performed calculations with FMA and one hydrogen-bonded water molecule, using the CASSCF/CASPT2 method. He found a transition energy of  $48,635 \text{ cm}^{-1}$  (0.01) for the  $n \rightarrow \pi^*$  transition and  $60,653 \text{ cm}^{-1}$  (0.34) for the  $\pi \rightarrow \pi^*$  transition of FMA. The  $n \rightarrow \pi^*$  transition was blueshifted by  $1,452 \text{ cm}^{-1}$ , while the  $\pi \rightarrow \pi^*$  transition was redshifted by  $1,210 \text{ cm}^{-1}$  relative to the gas phase, due only to the hydrogen bond with water. Besley and Hirst [7] have investigated the electronic spectrum of FMA in water, performing CASSCF/CASPT2 calculations within a self-consistent reaction field, with a repulsive potential to account for the Pauli repulsion between the solute and solvent. They found good agreement with the available experimental data, for the transitions involving valence and Rydberg states. These same authors have reported, more recently, the electronic spectrum of FMA in solution, using FMA-( $\text{H}_2\text{O}$ ) $_n$  ( $n = 1-3$ ) complexes within a continuum dielectric [9]. They found that the presence of explicit water molecules destabilizes the Rydberg states of FMA by approximately  $4,000 \text{ cm}^{-1}$ . The valence  $\pi \rightarrow \pi^*$  transition suffers a redshift of  $2,016 \text{ cm}^{-1}$  relative to the gas phase, with an increase of about 10% in its oscillator strength. The  $n \rightarrow \pi^*$  transition undergoes a blueshift of  $2,904 \text{ cm}^{-1}$  for the FMA-( $\text{H}_2\text{O}$ ) $_1$  complex, increasing as the number of water molecules increases. The results reported so far for the solvatochromic shift of the  $n \rightarrow \pi^*$  transition of FMA in water lies within the range  $1,452-3,549 \text{ cm}^{-1}$  for one [25] and three [26] hydrogen-bonded water molecules. There is a common sense between these previous works that to model the solvatochromic shift of the  $n \rightarrow \pi^*$  transition of FMA in water, it may be necessary to consider more explicitly defined solvent molecules and many solvent configurations. In fact, it is clear that optimized hydrogen-bonded clusters do not represent the real situation in a liquid. Further, in a liquid all properties are configurational averages and the system is characterized by a large number of structures at a certain temperature.

In the present work we address to the electronic spectrum of FMA in aqueous solution, using a sequential Monte Carlo/quantum mechanical (S-MC/QM) procedure [27, 28, 29]. We perform a systematic study of the solvent effects on the valence  $n \rightarrow \pi^*$  and  $\pi \rightarrow \pi^*$  electronic transitions of FMA, where the solvent molecules are explicitly included in the QM calculations. In this approach we use MC simulations to generate structures of the liquid and subsequently perform QM calculations on those supermolecular structures, with all-valence electrons, to obtain the separate contributions of the different solvation shells to the specific electronic transition. The number of necessary solvation shells to be included can be analyzed systematically and converged results obtained

[28]. As the number of configurations generated by the MC simulation is very high, the number of configurations to be submitted to subsequent QM calculations can be drastically reduced considering the statistical correlation between successive configurations generated by the MC simulations [27, 28, 30, 31]. In doing so, we are able to analyze the solvent effects varying from specific hydrogen-bond interactions up to the bulk limit. The largest calculation involves the ensemble average of 75 QM calculations performed on statistically uncorrelated structures obtained with the FMA solute surrounded by as many as 150 water solvent molecules. As presented later, the calculated values given for the solvatochromic shifts are statistically converged values. They are also converged with respect to the number of molecules included in each supermolecule. At the present stage, these large supermolecular QM calculations can only be made using semiempirical methods. The QM calculations start with a self-consistent-field intermediate neglect of differential overlap (INDO) calculation with a properly antisymmetric wavefunction with all valence electrons. The transition energies are obtained next using singly excited configuration interaction (CIS). As the number of solvent molecules explicitly included in the QM calculations is changed, the use of an extensive theory, such as CIS, is recommended. The S-MC/QM procedure differs from the conventional QM/MM method [32, 33, 34] in that all molecules –solute and solvent–are treated by quantum mechanics. The classical MC part is used only to generate the statistical structure of the liquid. Another important point is that all statistical information is obtained before running into the QM stage. This procedure has been successfully applied to study the solvent effects on the electronic spectrum of several systems, such as benzene [28] and  $\beta$ -carotene [29] in several different solvents, formaldehyde in water [35, 36], pyrimidine in water and in  $\text{CCl}_4$  [37], acetone in water [38] and *N*-methylacetamide in water [39].

## 2 Theoretical methodology

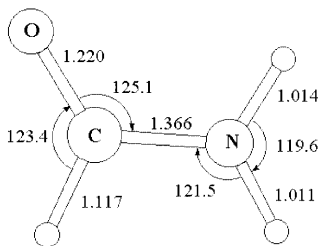
MC statistical mechanics simulations were carried out employing standard procedures [40], including the Metropolis sampling technique and periodic boundary conditions using the minimum image method in a cubic box. The simulations were performed in the canonical (NVT) ensemble. The system consisted of one FMA molecule plus 400 solvent molecules (water). The volume of the cubic box was determined by the experimental density of water, which at 298.15 K is  $0.9966 \text{ g cm}^{-3}$ . The intermolecular interactions are described by the standard Lennard-Jones plus Coulomb potential with three parameters for each atom  $i$  ( $\epsilon_i$ ,  $\sigma_i$  and  $q_i$ ). For the water molecules we used the simple point charge potential developed by van Gunsteren et al. [41]. For FMA, we used the optimized potential for liquid simulations potential [42], with the charges computed using the CHELPG fitting procedure [43], at the MP2/cc-pVDZ level of theory (Table 1). The intermolecular interactions were spherically truncated within a center-of-mass separation smaller than the cutoff radius,  $r_c$ , of 11.47 Å. Long-range corrections of the Lennard-Jones potential were calculated beyond this cutoff distance. In the simulation the molecules were kept with rigid geometries. The water molecules were kept in their  $C_{2v}$  structure with  $r_{\text{OH}} = 1.000 \text{ Å}$  and  $\angle\text{HOH} = 109.47^\circ$ . The FMA molecule was held rigid in its structure, optimized at the MP2/cc-pVDZ(d) level of theory, as shown in Fig. 1. The initial configurations were generated randomly, considering the position and orientation of each

**Table 1.** Intermolecular potential parameters used in the Monte Carlo simulations ( $q_i$  in elementary charge unit,  $\epsilon_i$  in kilocalories per mole and  $\sigma_i$  in angstroms)

Molecule	Site	$q_i$	$\epsilon_i$	$\sigma_i$
$\text{H}_2\text{O}^a$	O	-0.820	0.155	3.165
	H	0.410	0.000	0.000
$\text{HCNH}_2^b$	C	0.571	0.175	3.905
	N	-0.802	0.170	3.250
	O	-0.482	0.210	2.960
	H(CH)	-0.021	0.000	0.000
	H(NH)	0.367	0.000	0.000

<sup>a</sup> Simple point charge potential [41]

<sup>b</sup> Optimized potential for liquid simulation parameters [42] with the charges calculated using the CHELPG fitting procedure [43], at the MP2/cc-pVDZ level of theory



**Fig. 1.** MP2/cc-pVDZ optimized structural parameters for the formamide (FMA) molecule

molecule. The simulation consisted of a thermalization stage of  $4 \times 10^6$  MC steps, followed by an averaging of  $24 \times 10^6$  MC steps. To analyze the solvent effects on the electronic spectra of the FMA molecule we employed the S-MC/QM procedure [27, 28, 29], in which the QM calculations are performed on the supermolecular structures generated by the MC simulations. To analyze the convergence with the number of molecules included, the calculations were made with all solvent molecules within a particular solvation shell. Different solvation shells were considered. An important issue in all QM/MM methods is how to sample configurations from the statistical simulation. In our studies we sample configurations after analyzing the autocorrelation function of the energy [28, 30, 31, 35]. The use of the autocorrelation function of the energy for selecting configurations has been shown before to be an efficient procedure for obtaining converged average values [29, 30, 31]. In this present study we selected a total of 75 configurations, for each solvation shell, with less than 12% of statistical correlation. These configurations were used in the QM calculations. As we shall see later, the results obtained here are converged. The solvation shells were defined in the usual way, using the radial distribution function. The electronic spectra were then calculated using the semiempirical ZINDO [44] program, within the INDO/CIS [45] approach. As the appropriate Boltzmann weights are included in the Metropolis MC sampling technique, the average value of the transition energies and solvatochromic shifts are given as a simple average over the chain of calculated uncorrelated results.

All the ab initio calculations reported here were performed using the Gaussian98 program [46]. The MC statistical mechanics simulations were performed using the DICE program [47]. DICE is a general program for MC simulations that calculates thermodynamic properties and generates structures for use in most conventional quantum chemistry programs.

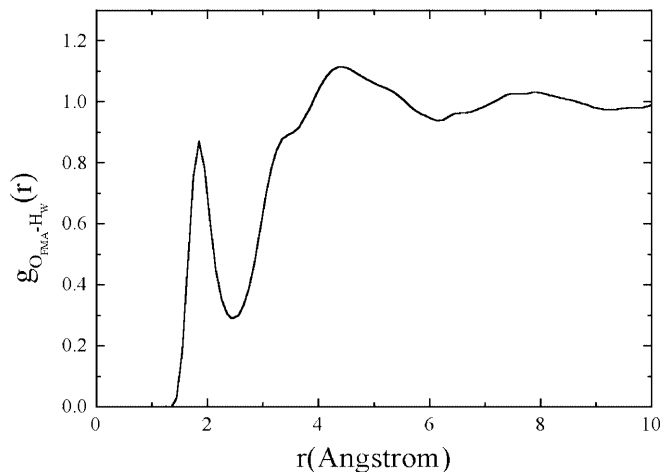
### 3 Results and discussion

#### 3.1 Hydrogen bond

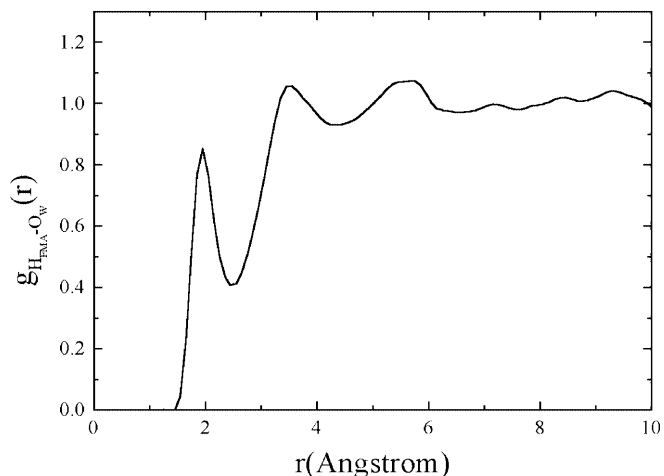
An important point in the solvation of FMA in water is the formation of hydrogen bonds. The radial pair

distribution function between the carbonyl oxygen of FMA and the water hydrogen,  $g_{\text{O-H}}(r)$ , is shown in Fig. 2 and the radial pair distribution function between the amino hydrogen of FMA and the water oxygen,  $g_{\text{H-O}}(r)$ , is shown in Fig. 3. Hydrogen-bonded structures are conventionally obtained from the analysis of the radial distribution functions  $g_{\text{O-H}}(r)$  and  $g_{\text{H-O}}(r)$  and these are shown in Figs. 2 and 3. The first peak in the  $g_{\text{O-H}}(r)$  distribution function starts at 1.45 Å, reaches its maximum at 1.85 Å and ends at 2.55 Å. For  $g_{\text{H-O}}(r)$ , the first peak starts at 1.55 Å, passes through a maximum at 1.95 Å and ends at 2.55 Å. The spherical integration of the first peak in  $g_{\text{O-H}}(r)$  and  $g_{\text{H-O}}(r)$  over the corresponding intervals gives 1.0 and 0.9 water molecules as nearest neighbors, respectively.

Hydrogen bonds in liquids are better obtained using geometric and energetic criteria, as discussed before by Stlinger and Rahman [48] and Mezei and Beveridge [49]. Indeed, these are more appropriate [48, 49, 50] to study solvent effects in spectroscopy [35]. We consider here a hydrogen-bond formation when the distance  $R_{\text{DA}} \leq 4$  Å,



**Fig. 2.** Radial pair distribution function between the carbonyl oxygen of FMA and the hydrogen of water



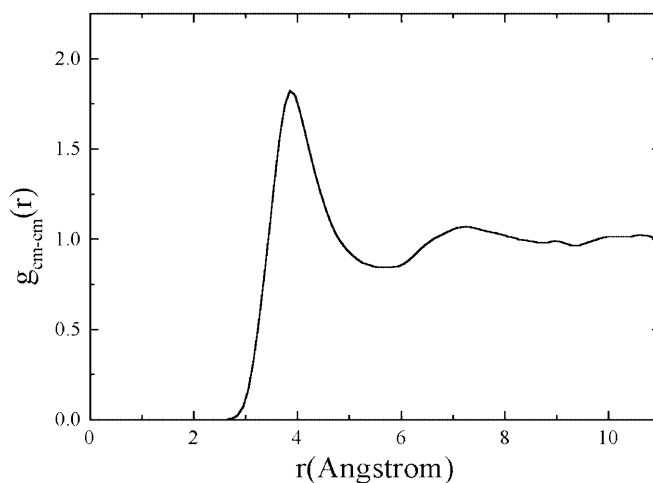
**Fig. 3.** Radial pair distribution function between the hydrogen atom of FMA (N-H) and the oxygen atom of water

the angle  $\angle AHD \leq 30^\circ$  and the binding energy is higher than  $3.0 \text{ kcalmol}^{-1}$ . In doing so, in the 75 MC configurations we find 109 hydrogen bonds formed between FMA and water molecules. This gives an average of 1.5 hydrogen bonds. Note that these are averages for the liquid. FMA can form up to three hydrogen bonds with the surrounding water molecules and the statistics obtained for the hydrogen bonds formed are given in Table 2. We find that in 12% of the configurations, FMA does not form hydrogen bonds, in 43% it forms one, in 33% it forms two and in 12% it forms three hydrogen bonds. The average classical values computed for the hydrogen binding energy when the carbonyl oxygen of FMA acts as a proton acceptor and when the NH group acts as a proton donor are  $6.1$  and  $5.0 \text{ kcalmol}^{-1}$ , respectively.

### 3.2 Electronic spectrum

The calculated solvatochromic shifts on the electronic transitions of FMA, due only to the hydrogen bonds between FMA and water, are also shown in Table 2. The  $n \rightarrow \pi^*$  transition of FMA suffers a blueshift of  $310 \text{ cm}^{-1}$  due only to one hydrogen-bonding interaction. The blueshift increases as the number of hydrogen bonds increases, being  $432$  and  $850 \text{ cm}^{-1}$  due to two and three hydrogen bonds, respectively. Similar trends are observed for the  $\pi \rightarrow \pi^*$  transition which undergoes a redshift of  $116 \text{ cm}^{-1}$  due to one hydrogen-bond interaction and increases to  $385$  and  $1101 \text{ cm}^{-1}$  due to two and three hydrogen bonds, respectively. On average, the hydrogen-bond shell contributes  $379 \pm 58 \text{ cm}^{-1}$  to the blueshift of the  $n \rightarrow \pi^*$  transition and  $320 \pm 96 \text{ cm}^{-1}$  to the redshift of the  $\pi \rightarrow \pi^*$  transition of FMA. Note that these hydrogen-bond contributions given in Table 2 are obtained using the structures obtained from the liquid. These structures give a solvation shift that is considerably smaller than that obtained using optimized clusters. Again, in the liquid the results, as reported here, are obtained using averages of different structures generated at room temperature. To analyze the effect on the number of molecules around the FMA molecule we use the radial distribution function,  $g(r)$ , of the center of masses.  $g_{\text{cm-cm}}(r)$  calculated for the FMA molecule in

water solution is depicted in Fig. 4, where two solvation shells are easily distinguished. The first solvation shell starts at  $2.65 \text{ \AA}$  and extends up to  $5.75 \text{ \AA}$ ; the second solvation shell ends at  $8.65 \text{ \AA}$ . Spherical integration of  $g_{\text{cm-cm}}(r)$  over the corresponding intervals gives 25 and 96 water molecules in the first and second solvation shells, respectively. Since the liquid is not structured beyond the second solvation shell, to go beyond we used solvent molecules up to a maximum of 150 water molecules. This corresponds to all water molecules within a radius of  $10.25 \text{ \AA}$ . For each shell 75 QM calculations of the electronic spectrum were performed and the values of the transition energies were averaged out. The results obtained are reported in Table 3. Our largest calculation, made for the outermost shell, includes one FMA molecule and 150 water molecules, with 1,218 valence electrons explicitly included. The corresponding calculated shifts for the  $n \rightarrow \pi^*$  and  $\pi \rightarrow \pi^*$  transitions of FMA in these largest structures are  $1,558 \pm 59$  and  $-757 \pm 65 \text{ cm}^{-1}$ , respectively. The results in Table 3 show that the solvatochromic shifts are nearly converged with respect to the number of water molecules included in the supermolec-



**Fig. 4.** Radial pair distribution function between the FMA center of mass and the water center of mass

**Table 2.** Statistics of the hydrogen bonds formed between formamide (FMA) and water and their contribution to the solvatochromic shifts of the  $n \rightarrow \pi^*$  and  $\pi \rightarrow \pi^*$  transitions. The absolute intermediate neglect of differential overlap (INDO)/singly excited configuration interaction (CIS) transition energies, computed in the gas phase, for the  $n \rightarrow \pi^*$  and  $\pi \rightarrow \pi^*$  transitions of FMA are  $36,100$  and  $60,503 \text{ cm}^{-1}$ , respectively, with oscillator strengths of  $0.001$  and  $0.320$ , respectively

Number of hydrogen bonds	Occurrence (%)	$n \rightarrow \pi^*$ shift ( $\text{cm}^{-1}$ )	$\pi \rightarrow \pi^*$ shift ( $\text{cm}^{-1}$ )
0	12	–	–
1	43	310	–116
2	33	432	–385
3	12	850	–1,101
Total	100	$379 \pm 58$	$-320 \pm 96$

**Table 3.** Variation of the calculated (INDO/CIS) shifts of the  $n \rightarrow \pi^*$  and  $\pi \rightarrow \pi^*$  transitions of FMA in water with the solvation shells.  $N$  is the total number of water molecules included.  $M$  is the total number of valence electrons included in the quantum mechanical calculations.  $r$  is the distance of the radial distribution function. Each solvatochromic shift shown is the result of an average of 75 quantum mechanical calculations. See text

$N$	$M$	$r$ ( $\text{\AA}$ )	$n \rightarrow \pi^*$ shift ( $\text{cm}^{-1}$ )	$\pi \rightarrow \pi^*$ shift ( $\text{cm}^{-1}$ )
25	218	5.75	$1,131 \pm 54$	$-558 \pm 72$
55	458	7.45	$1,347 \pm 54$	$-692 \pm 64$
96	786	8.85	$1,481 \pm 57$	$-770 \pm 68$
120	978	9.55	$1,529 \pm 57$	$-781 \pm 69$
150	1,218	10.25	$1,558 \pm 59$	$-757 \pm 65$
Limit			$1,600 \pm 59$	$-800 \pm 65$

ular structures. The calculated solvatochromic shifts for the  $n \rightarrow \pi^*$  and  $\pi \rightarrow \pi^*$  transitions of FMA as a function of the number of water molecules included can be seen in Fig. 5. The monotonic behavior of the calculated energy shift for the  $n \rightarrow \pi^*$  and  $\pi \rightarrow \pi^*$  transitions of FMA permits the extrapolation of the results to the bulk limit. In doing so we obtain limiting values of 1,600 and  $-800 \text{ cm}^{-1}$  for the  $n \rightarrow \pi^*$  and  $\pi \rightarrow \pi^*$  transitions. This would be our best estimate for the solvatochromic shifts of the  $n \rightarrow \pi^*$  and  $\pi \rightarrow \pi^*$  electronic transitions of FMA in aqueous solution. Unfortunately an experimental value is not available for comparison. These numbers are however in close agreement with those obtained in a similar study for *N*-methylacetamide [39].

The solvatochromic shift of the  $n \rightarrow \pi^*$  transition, due only to the hydrogen-bond interactions, represents about 20% of the total shift extrapolated to the bulk limit. For the  $\pi \rightarrow \pi^*$  transition, hydrogen bonds contributes to about 30% of the total shift. Our results obtained for the hydrogen-bond contribution to the solvent shifts of the  $n \rightarrow \pi^*$  and  $\pi \rightarrow \pi^*$  transitions of FMA in aqueous solution are lower when compared

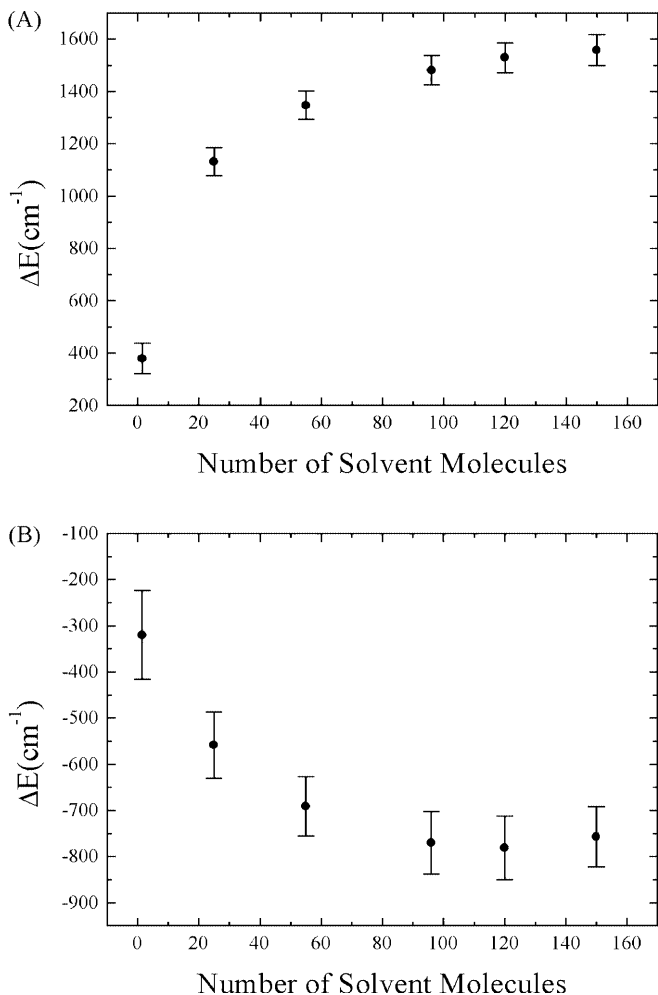
with previous results for FMA-( $\text{H}_2\text{O}$ ) $_n$  ( $n = 1-3$ ) cluster calculations [9, 24, 25, 26]. However, it is important to realize that in the cluster the hydrogen-bond interaction is stronger than in the liquid, as in this case the water is also bound to other water molecules. Another aspect is that in the liquid several structures are possible at a given temperature and not only a minimum energy as in the case of the optimized cluster. As a result, the calculation using the optimized gas-phase structure overestimates the hydrogen bond and does not reproduce the situation of the liquid. This has been noted before for acetone in water [38].

### 3.3 Sampling and statistical convergence

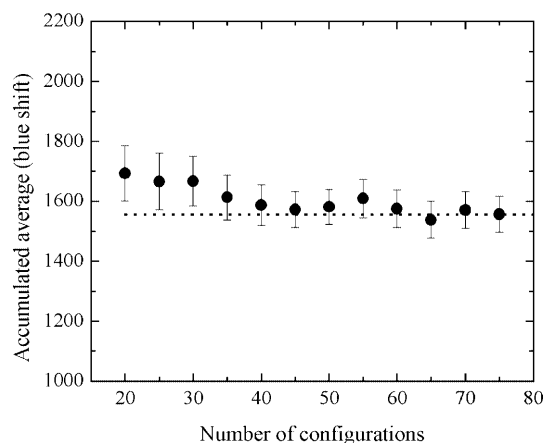
As the calculated average values obtained here are derived from several QM calculations using the structures of the simulation, it is important now to discuss the convergence of the final result. It is also convenient to show the statistical efficiency obtained with the autocorrelation function of the energy. In doing so, the subsequent QM calculations are performed only on some uncorrelated structures. This is one of the advantages of the S-MC/QM procedure, in that all the important MC statistical information is available before running into the QM calculations. As in previous work [28, 29, 30, 31, 35, 36, 37] we calculate the autocorrelation function of the energy,  $C(n)$ , to obtain the interval of statistical correlation, using the definition

$$C(n) = \frac{\langle \delta E_i E_{i+n} \rangle}{\langle \delta E^2 \rangle} = \frac{\sum_i (E_i - \langle E \rangle)(E_{i+n} - \langle E \rangle)}{\sum_i (E_i - \langle E \rangle)^2},$$

where  $E_i$  is the energy of configuration  $i$  and  $E_{i+n}$  is the energy of the configuration generated  $n$  MC steps later. For Markovian processes, it is known that  $C(n)$  follows an exponential decay [28, 35],  $C(n) = \exp(-n/\tau)$ , and represents the statistical correlation between configurations separated by  $n$  MC steps. In practice, the configurations are considered statistically uncorrelated for an interval  $n \approx 2\tau$ . For FMA in water, we find that configurations separated by  $3.2 \times 10^5$  MC steps are 10% correlated. Using configurations separated by much less than this is a waste because the calculation includes configurations that do not contribute to the average. Thus, out of the simulation of  $24 \times 10^6$  MC steps we use only 75 configurations. The dependence of our calculated solvation shift on the number of configurations used for the  $n \rightarrow \pi^*$  transition is shown in Fig. 6. The results show the convergence of the average value. This is a demonstration of the efficiency of the use of the autocorrelation function in that only a few instantaneous values give statistically converged results. Thus, the use of the interval of the statistical correlation ( $2\tau$ ) obtained using the autocorrelation function of the energy is a very effective way to sample configurations giving statistically converged results with a relatively small number of calculations, because only statistically relevant configurations are included. Our present results



**Fig. 5.** Calculated solvatochromic shift for **A** the  $n \rightarrow \pi^*$  and **B** the  $\pi \rightarrow \pi^*$  transition of FMA in water, as a function of the number of solvent molecules



**Fig. 6.** Convergence of the calculated solvation shifts ( $\text{cm}^{-1}$ ) of the  $n \rightarrow \pi^*$  transition of FMA in water

are converged values incorporating the inherent statistical nature of the liquid.

#### 4 Summary and conclusions

In this work we employed a S-MC/QM procedure to analyze the solvent effects on the  $n \rightarrow \pi^*$  and  $\pi \rightarrow \pi^*$  electronic transitions of FMA in aqueous solution. The structural analysis of the solution, by means of the radial pair distribution function, showed that FMA can form up to three hydrogen bonds with water. The hydrogen-bond statistics revealed that in 12% of the configurations FMA does not form any hydrogen bonds with water, but in 43% forms one, in 33% forms two and in 12% forms three hydrogen bonds. The  $n \rightarrow \pi^*$  transition of FMA suffers a blueshift of  $379 \pm 58 \text{ cm}^{-1}$  due only to hydrogen-bonding interactions. Similarly, the  $\pi \rightarrow \pi^*$  transition undergoes a redshift of  $320 \pm 96 \text{ cm}^{-1}$ . Next, 75 QM calculations were made for each of the first, second and outer solvation shells. To verify convergence with the number of molecules included in the supermolecules, calculations were made including all water molecules up to the limit radius of 10.25 Å. We find that the  $n \rightarrow \pi^*$  transition suffers a blueshift of  $1,600 \text{ cm}^{-1}$  upon solvation and the  $\pi \rightarrow \pi^*$  transition undergoes a redshift of  $800 \text{ cm}^{-1}$ . Statistical convergence is obtained using the autocorrelation function of the energy to sample the configurations from the MC simulation. The solvation shifts reported here are thus converged values both with respect to the number of molecules explicitly included as well as the number of configurations used for the statistical averages. The sequential use of the MC and QM calculations allows the advantageous use of the statistical information before the QM calculations. Also, all molecules within a particular supermolecular structure are treated by quantum mechanics, thus including the important polarization effects.

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